Drought severity–duration–frequency curves: a foundation for risk assessment and planning tool for ecosystem establishment in post-mining landscapes

D. Halwatura¹, A. M. Lechner²,³, and S. Arnold¹

¹Centre for Mined Land Rehabilitation, Sustainable Minerals Institute, the University of Queensland, Brisbane, Australia
²Centre for Social Responsibility in Mining, Sustainable Minerals Institute, the University of Queensland, Brisbane, Australia
³Centre for Environment, University of Tasmania, Hobart, Australia

Correspondence to: D. Halwatura (d.halwatura@uq.edu.au)

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Abstract. Eastern Australia has considerable mineral and energy resources, with areas of high biodiversity value co-occurring over a broad range of agro-climatic environments. Lack of water is the primary abiotic stressor for (agro)ecosystems in many parts of eastern Australia. In the context of mined land rehabilitation quantifying the severity–duration–frequency (SDF) of droughts is crucial for successful ecosystem rehabilitation to overcome challenges of early vegetation establishment and long-term ecosystem resilience.

The objective of this study was to quantify the SDF of short-term and long-term drought events of 11 selected locations across a broad range of agro-climatic environments in eastern Australia by using three drought indices at different timescales: the Standardized Precipitation Index (SPI), the Reconnaissance Drought Index (RDI), and the Standardized Precipitation-Evapotranspiration Index (SPEI). Based on the indices we derived bivariate distribution functions of drought severity and duration, and estimated the recurrence intervals of drought events at different timescales. The correlation between the simple SPI and the more complex SPEI or RDI was stronger for the tropical and temperate locations than for the arid locations, indicating that SPEI or RDI can be replaced by SPI if evaporation plays a minor role for plant available water (tropics). Both short-term and long-term droughts were most severe and prolonged, and recurred most frequently in arid regions, but were relatively rare in tropical and temperate regions.

Our approach is similar to intensity–duration–frequency (IDF) analyses of rainfall, which are crucial for the design of hydraulic infrastructure. In this regard, we propose to apply SDF analyses of droughts to design ecosystem components in post-mining landscapes. Together with design rainfalls, design droughts should be used to assess rehabilitation strategies and ecological management using drought recurrence intervals, thereby minimising the risk of failure of initial ecosystem establishment due to ignorance of fundamental abiotic and site-specific environmental barriers, such as flood and drought events.

1 Introduction

Eastern Australia holds vast mineral and energy resources of economic importance and internationally significant biodiversity (Williams et al., 2002; Myers et al., 2000) occurs over a broad range of agro-climatic environments (Hutchinson et al., 2005; Woodhams et al., 2012). There are also extensive areas of cropping and grazing such as in the Brigalow Belt Bioregion (Arnold et al., 2013) and the wheatbelt regions around Kingaroy and Wagga Wagga (Woodhams et al., 2012) (Table 1, Fig. 1). Lack of water availability is a critical factor for the mining industry, agriculture and biodiversity. For example, water deficit reduces agricultural productivity and increases the risk of failure of ecosystem rehabilitation. Likewise, flooding affects mining as a result of soil erosion in rehabilitation areas or flooded mine sites pre-
Droughts and associated limitations in plant available water determine plant distribution in response to climatic conditions in post-mining landscapes. Ecosystem attributes such as the distribution of native tropical species (Engelbrecht et al., 2007; Kuster et al., 2013), the structure and functioning of forests (Zhang and Jia, 2013; Vargas et al., 2013), biodiversity and ecosystem resilience (Brouwers et al., 2013; Lloret, 2012; Jongen et al., 2013), and primary productivity and respiration of vegetation (Shi et al., 2014) are sensitive to the occurrence of drought events. In the context of mined land rehabilitation, droughts also play a critical role for the early establishment of plants (Nefzaoui and Ben Salem, 2002; Gardner and Bell, 2007) and long-term resilience of novel ecosystems on post-mining land (Bell, 2001). Across the life span of plants due to their under-developed root system, juvenile vegetation such as seeds, seedlings, and pre-mature rather than climax vegetation is especially vulnerable to lack of water availability (Jahantab et al., 2013; Craven et al., 2013; Arnold et al., 2014a). For climax vegetation, however, medium to long-term drought (greater than 9 months) periods rather than short-term droughts (3 months or less) may critically impact rehabilitation by altering plant communities’ species composition (Mariotte et al., 2013; Ruffault et al., 2013).

Droughts are usually characterised through the use of indices, which vary in complexity and data needs. Meteorological or climatological droughts are the simplest and are based on the characterisation of anomalies in rainfall conditions (Anderegg et al., 2013). For meteorological droughts, standardised drought indices such as the Standardized Precipitation Index (SPI), Reconnaissance Drought Index (RDI) and Standardized Precipitation-Evapotranspiration Index (SPEI) provide the means to quantifying the duration and severity, and eventually the frequency or recurrence of drought events (McKee et al., 1993; Tsakiris and Vangelis, 2005; Vicente-Serrano et al., 2010). Although there are numerous comparative studies of drought indices in certain climatic regions such as the Mediterranean, (Paulo et al., 2012; Livada and Assimakopoulos, 2007), the Carpathian region (Spinoni et al., 2013), and other arid locations (Peel et al., 2007; Zarch et al., 2011), none of these indices apply universally to any climate region and it is best for land managers to use a range of drought indices at various temporal scales (Heim, 2002; Spinoni et al., 2013). In many parts of the world evaporation data are unavailable or incomplete and simple rainfall indices such as SPI are most commonly used. In this study, we compare SPI with RDI at the 3-month timescale and SPI and SPEI at the 12-month timescale to determine the difference between using SPI with more complex indices that incorporate evaporation in different climatic regions.

Drought periods can be characterised from a few hours (short-term) to millennia (long-term) depending on the ecological or socio-economic question being addressed. The time lag between the beginning of a period of water scarcity and its impact on socio-economic and/or environmental assets is referred to as the timescale of a drought (Vicente-Serrano et al., 2013). There are three timescales for which drought indices are usually calculated; short-term droughts are 3 months or less; medium-term droughts are between 4 to 9 months; and long-term droughts are 12 months or more (Zargar et al., 2011). Short-term droughts have an impact on water availability in the vadose zone (National Drought Mitigation Center, 2014; Zargar et al., 2011), while long-term droughts also affect surface and ground water resources (National Drought Mitigation Center, 2014; Zargar et al., 2011).

Of key importance for land managers planning for drought events of any timescale is characterising the return period or...
Table 1. Climate indices and classification of selected locations across eastern Australia with focus on rainfall.

| Location                  | Length of meteorological data (years) | Climate index | Climate classification system | Potential productive land use  
<table>
<thead>
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<tbody>
<tr>
<td></td>
<td></td>
<td>$R/PET^a$</td>
<td>$R_w/R_s^b$</td>
<td></td>
</tr>
<tr>
<td>Weipa</td>
<td>1960–1994 (34)</td>
<td>0.99</td>
<td>0.01</td>
<td>Tropical, savannah</td>
</tr>
<tr>
<td>Cairns</td>
<td>1965–2013 (48)</td>
<td>0.91</td>
<td>0.10</td>
<td>Tropical, savannah</td>
</tr>
<tr>
<td>Brisbane</td>
<td>1986–2013 (27)</td>
<td>0.55</td>
<td>0.38</td>
<td>Temperate, without dry season</td>
</tr>
<tr>
<td>Sydney</td>
<td>1970–1994 (24)</td>
<td>0.53</td>
<td>0.51</td>
<td>Temperate, without dry season</td>
</tr>
<tr>
<td>Melbourne</td>
<td>1955–2013 (58)</td>
<td>0.51</td>
<td>0.95</td>
<td>Temperate, without dry season</td>
</tr>
<tr>
<td>Kingaroy</td>
<td>1967–2001 (34)</td>
<td>0.47</td>
<td>0.34</td>
<td>Temperate, without dry season</td>
</tr>
<tr>
<td>Brigalow Research Station</td>
<td>1968–2011 (43)</td>
<td>0.32</td>
<td>0.27</td>
<td>Temperate, without dry season</td>
</tr>
<tr>
<td>Wagga Wagga</td>
<td>1966–2013 (47)</td>
<td>0.30</td>
<td>1.21</td>
<td>Temperate, without dry season</td>
</tr>
<tr>
<td>Bourke</td>
<td>1967–1996 (29)</td>
<td>0.20</td>
<td>0.61</td>
<td>Arid, steppe</td>
</tr>
<tr>
<td>Quilpie</td>
<td>1970–2013 (43)</td>
<td>0.14</td>
<td>0.36</td>
<td>Arid, steppe</td>
</tr>
<tr>
<td>Mount Isa</td>
<td>1975–2013 (38)</td>
<td>0.13</td>
<td>0.05</td>
<td>Arid, steppe</td>
</tr>
</tbody>
</table>

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$^a$ Unep and Thomas (1992); $^b$ based on average of 3 months of rainfall during winter (June–August) and summer (December–February); $^c$ Peel et al. (2007); $^d$ Woodhams et al. (2012); $^e$ Hutchinson et al. (2005).
frequency of occurrence of rainfall and drought events. The recurrence interval is defined as the average inter-occurrence time of any geophysical phenomena and is calculated with long-term time series data (Loaiciga and Mariño, 1991). Recurrence intervals of rainfall events greater than the average are commonly used by engineers to derive intensity–duration–frequency (IDF) design estimates for building hydraulic infrastructure such as roofs, culverts, stormwater drains, bridges or water dams (Chebbi et al., 2013; Kuo et al., 2013; Hailegeorgis et al., 2013). IDF design rainfalls are crucial for estimating the risk of hydraulic infrastructure failure and for maximising infrastructure efficiencies (Smithers et al., 2002). Similar to the concept of IDF design rainfall, which aims to quantify the recurrence interval of rainfall events based on their intensity and duration, we apply the same concept to quantify the recurrence intervals of droughts based on their severity and duration, and refer to this as severity–duration–frequency (SDF) design drought. SDF curves have been used to derive drought variables (severity, duration, frequency of occurrence) in different climatic regions (Shiau, 2006; Shiau et al., 2012; Lee and Kim, 2012; Todisco et al., 2013; Mirabbasi et al., 2012) but have rarely been used in ecology, and never been used in relation to rehabilitation and restoration. While IDF design rainfalls are a well-established tool in civil engineering and hydrology, we believe SDF design drought could be used in a similar way to assess the risk of ecosystem rehabilitation failure due to droughts.

This approach contrasts current climate classification methods (Table 1) such as the classification of the Australian agricultural environments (Woodhams et al., 2012) or the Australian agro-climatic classes (Hutchinson et al., 2005) that are used for the management of agricultural land (Audet et al., 2013). These classifications are based on average climatic conditions and may not be adequate for the management of early vegetation re-establishment in post-mining landscapes (Audet et al., 2012, 2013) because of the vulnerability of vegetation to drought events. Although droughts play a critical role in post-mining land restoration in eastern Australia, so far methods for quantifying the frequency of drought events have been rarely applied to assess the risk of failure of ecosystem rehabilitation. In the perspective of mined land rehabilitation, specific metrics of site climate or seasonality are surprisingly rare (Audet et al., 2013).

The objective of our study is to quantify the severity, duration, and frequency (SDF) of short-term and long-term drought events at selected locations across a broad range of agro-climatic environments in eastern Australia (Table 1, Fig. 1). Eastern Australia makes a very good case study for this kind of research as there are a wide range of climates in which data has been gathered using a consistent method by one agency. While other studies assessed the SDF characteristics at locations with the same climate in Iran (Shiau and Modarres, 2009; Shiau et al., 2012), no such investigations are known for any climatic region in Australia, for the same climate or different climates.

We characterised droughts using the RDI and SPEI for 3- and 12-month timescales respectively, and compared these indices with the SPI at the same timescales. We then linked the univariate distributions of severity and duration calculated with the drought indices to form bivariate distribution functions and estimated the recurrence intervals of droughts. Please note that since the estimated recurrence intervals are based on historic rainfall and evaporation data, our results are descriptive rather than predictive. Nevertheless, our findings are crucial to discuss the potential of design droughts to be applied as a management tool to overcome the challenges of early vegetation establishment and long-term ecosystem resilience in post-mining landscapes. This is because frequency patterns of drought events are ignored in any current rehabilitation guidelines and industry plans, where long-term average rainfall is the only parameter upon which management decisions are based on (Audet et al., 2013).

2 Materials and methods

Estimating SDF curves involves uncertainties associated with the length of the observed rainfall data, the applied drought index, the probability distribution functions used to fit the observed severity and duration, and the estimated copula parameter (Hu et al., 2014). To overcome these uncertainties we tested the applicability of drought indices for locations in different climatic regions by calculating the correlation of three selected drought indices. Likewise, we used the best fitted probability distribution functions and copula for each site. A flow chart of the processing steps is depicted in a schematic diagram (Fig. 2).

We selected 11 sites, for which historical observations of monthly rainfall and evaporation (ranging from 30–60 years) (Table 1) were most comprehensive (more than 97 % coverage) (i.e. longest and most complete – more than 97 % coverage) across eastern Australia (Bureau of Meteorology, 2013). The selected locations covered a broad range of climate classes and environments across eastern Australia (Table 1, Fig. 1).

For each site we compared the simple SPI with the more complex RDI and SPEI drought indices. Amongst the three indices, the SPI is the most widely used and simplest drought index, because it is solely based on long-term rainfall for any period of interest (McKee et al., 1993; Guttman, 1999). However, SPI may not adequately characterise drought events, because it does not incorporate other meteorological data (Vicente-Serrano et al., 2010; Mishra and Singh, 2010). Both the RDI and SPEI integrate potential evaporation and thereby better represent the local water balance (Tsakiris, 2004; Tsakiris and Vangelis, 2005; Tsakiris et al., 2007; Vangelis et al., 2013).
The drought indices are calculated using monthly values of rainfall and/or potential evaporation. Amongst the two indices which incorporate potential evaporation, the RDI plays a strong role in detecting maximum drought severities at the medium timescale (3 to 6 months) (Banimahd and Khalili, 2013), while the SPEI plays a strong role in detecting annual drought events by identifying the hydrological summer drought events (Egidijus et al., 2013). There is evidence that SPI overestimates small rainfall scarcity even if excessive rainfall occurs just before the period of interest (Kim et al., 2009). Also for humid climates, there is a good correspondence between the computed SPI and RDI (Khalili et al., 2011). For Mediterranean climate, SPI and SPEI at 9- and 12-month timescales are well correlated (Paulo et al., 2012), and
in the Carpathian region SPI, SPEI, and RDI are highly comparable over annual periods (Spinoni et al., 2013). In arid regions, the correlation of SPI and RDI is more considerable at the 3-, 6-, and 9-monthly timescale (Peel et al., 2007; Zarch et al., 2011).

2.1 Step 1: calculate drought indices

The SPI is derived by fitting a probability distribution to the rainfall record and then transforming that to a normal distribution, so that mean and standard deviation of the SPI are zero and one. Positive or negative values of the SPI represent rainfall conditions greater or smaller than average rainfall, respectively (McKee et al., 1993). RDI and SPEI are based on the SPI calculation procedure, except the two indices use the quotient or difference of precipitation and potential evaporation, respectively (Tsakiris et al., 2007; Vicente-Serrano et al., 2010). Equations for the RDI and SPEI are presented in Appendix A. We applied two correlation coefficients to assess the correlations between SPI

\[ I, \text{ and } D \]

and severity

\[ S, \text{ and } D \]

of the drought indices (McKee et al., 1993; Vicente-Serrano et al., 2010; Tsakiris and Vangelis, 2005). The duration of any drought was defined as the period of rainfall deficit, i.e. the cumulative time of negative \( I \) values preceded and followed by positive \( I \) values (Fig. 3). The severity of any drought period starting at the \( i \)th month was defined as

\[
S = \sum_{i=1}^{D} | -I_i |. \tag{1}
\]

We fitted the time series of \( D \) and \( S \) to a range of cumulative distribution functions (gamma, logistic, extreme value, lognormal, bimodal lognormal, and exponential) and used the function with the best fit for further investigations (step 2 in Fig. 2). The coefficient of determination and 95 \% confidence levels were calculated for each distribution in order to select the best distribution.

2.2 Step 2: bivariate distribution of drought severity and duration

For each location, we used the estimated drought indices (SPI, RDI, SPEI), hereafter collectively referred to as \( I, \text{ to quantify duration } D \text{ and severity } S \) (McKee et al., 1993; Vicente-Serrano et al., 2010; Tsakiris and Vangelis, 2005). The duration of any drought was defined as the period of rainfall deficit, i.e. the cumulative time of negative \( I \) values preceded and followed by positive \( I \) values (Fig. 3). The severity of any drought period starting at the \( i \)th month was defined as

\[
S = \sum_{i=1}^{D} | -I_i |. \tag{1}
\]

We fitted the time series of \( D \) and \( S \) to a range of cumulative distribution functions (gamma, logistic, extreme value, lognormal, bimodal lognormal, and exponential) and used the function with the best fit for further investigations (step 2 in Fig. 2). The coefficient of determination and 95 \% confidence levels were calculated for each distribution in order to select the best distribution.

2.3 Step 3: estimate copula parameter

We used copulas to link the univariate probability distributions of \( D \) and \( S \) to construct a bivariate joint distribution of \( D \) and \( S \) (Shiau and Modarres, 2009; Sklar, 1959) (step 3 in Fig. 2). As the choice of copula can be very different from one climate region to another (Khedun et al., 2013) the present study focused on the Frank and Gumbel copulas (Appendix B), as they perform best when analysing the bivariate drought dependence structure of drought variables such as severity and duration (Ganguli and Reddy, 2012; Reddy and Ganguli, 2012; Shiau, 2006; Lee et al., 2013; Wong et al., 2010; Zhang et al., 2011). The conditional cumulative distribution function \( F_{S|D}(s|d) \) which relates to the joint cumulative distribution function (JCDF) of severity and duration \( F_{S,D}(s, d) \) and the conditional cumulative distribution function (CDF) of drought duration \( F_D(d) \) is given by the following relationship (Shiau and Modarres, 2009):

\[
F_{S|D}(s|d) = \frac{\partial F_{S,D}(s, d)}{\partial F_D(d)}, \tag{2}
\]

where \( F_D(d) \) is the CDF of drought duration, and \( F_{S,D}(s, d) \) is the JCDF of drought severity and drought duration. The JCDF of drought severity and duration in terms of copulas is a function of univariate CDFs of duration and severity:

\[
F_{S,D}(s, d) = C(F_S(s), F_D(d)), \tag{3}
\]

where \( F_S(s) \) and \( F_D(d) \) are CDFs for drought severity and duration, respectively, and \( C \) is a copula function. The conditional distribution function \( F_{S|D}(s|d) \) (Eq. 2) can also be expressed as a function of the copula (Shiau and Modarres, 2009):

\[
F_{S|D}(s|d) = \frac{\partial F_{S,D}(s, d)}{\partial F_D(d)} = \frac{\partial C(F_S(s), F_D(d))}{\partial F_D(d)} = C_{F_S|F_D}(F_S(s) | F_D(d)). \tag{4}
\]

We estimated the copula parameters using the inference function for margins (IFM) (Joe, 1997). The IFM comprises two separate valuation stages. First, the maximum likelihood estimation of each univariate distribution is performed, and then the copula dependence parameter is estimated to derive the joint drought duration and severity distributions (Shiau, 2006; Shiau and Modarres, 2009; Mirabbasi et al., 2012; Shiau et al., 2007).
2.4 Step 4: derive recurrence intervals

We used the estimated copula parameters to generate random drought events. Severity and duration of the generated random droughts were then fitted to cumulative distribution functions in the same manner as in step 2 (Fig. 2, step 3) to test which estimated copula parameters result in a distribution that best fit the generated random drought variables. The estimated copula parameters were also assessed quantitatively through calculating the correlation between generated random drought events and the estimated gamma ($S$) and logistic ($D$) cumulative distribution functions.

The generated random numbers were then used to calculate the recurrence intervals. Recurrence intervals of bivariate drought events is a standard metric for hydrological frequency analysis (Yoo et al., 2013; Hailegeorgis et al., 2013) and water resources management (Shiau and Modarres, 2009; Mishra and Singh, 2010). For each location, we calculated the recurrence interval of drought events exceeding any severity $s$ or duration $d$, denoted by the logical operator “$\lor$”:

$$T_I^{\lor} = \frac{1}{P(S \geq s \lor D \geq d)} = \frac{1}{1 - C[F_S(s), F_D(d)]}$$

where $I$ is one of the drought indices of interest, i.e. the 12-monthly SPEI$_{12}$ or SPI$_{12}$, or the 3-monthly RDI$_3$ or SPI$_3$. Alternatively, the recurrence interval of drought events exceeding any severity $s$ and duration $d$, denoted by the logical operator “$\land$”, was calculated as

$$T_I^{\land} = \frac{1}{P(S \geq s \land D \geq d)} = \frac{1}{1 - F_S(s) - F_D(d) + C[F_S(s), F_D(d)]}$$

For the sake of simplicity, we only present and discuss $T_I^{\lor}$, whereas $T_I^{\land}$ is presented in Appendix D.

3 Results

For both indices, RDI and SPEI, and all selected sites, the gamma and logistic distributions fitted best to the observed drought severity and duration, respectively ($R^2 > 0.98$ for both variables, $p < 0.05$) (Appendix F). Likewise, the same distributions fitted best to the drought severity and duration of the generated drought events based on the Frank rather than the Gumbel copula ($R^2 > 0.90$, $p < 0.05$) (Appendix F).

Based on the drought indices RDI$_3$ and SPEI$_{12}$ we detected distinct drought patterns across the selected sites at short and long-term scales, respectively. As an example of differences between tropical, temperate and arid rainfall conditions, Fig. 4 depicts calculated time series of RDI$_3$ and SPEI$_{12}$ for Weipa, Sydney and Quilpie, respectively (see Appendix C for rest of the sites).

Short-term droughts were most severe and prolonged in tropical Weipa and Cairns, and temperate Wagga Wagga (Table 2). However, in contrast to Wagga Wagga, the two tropical locations were characterised by distinct seasonality patterns and very low variation as indicated by the low ratio of winter to summer rainfalls (Table 1) and low coefficients of variation in severity and duration (Table 2). The highest vari-
Table 2. Mean severity $\mu_s$ and duration $\mu_d$ of selected locations across eastern Australia, and corresponding coefficient of variation $CV_s$ and $CV_d$ for short-term (RDI$_3$) and long-term (SPEI$_{12}$) droughts.

<table>
<thead>
<tr>
<th>Location</th>
<th>RDI$_3$</th>
<th>SPEI$_{12}$</th>
<th>RDI$_3$</th>
<th>SPEI$_{12}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\mu_s$</td>
<td>CV$_s$</td>
<td>$\mu_d$</td>
<td>CV$_d$</td>
</tr>
<tr>
<td>Weipa</td>
<td>5.2</td>
<td>0.2</td>
<td>5.8</td>
<td>0.1</td>
</tr>
<tr>
<td>Cairns</td>
<td>4.7</td>
<td>0.4</td>
<td>6.4</td>
<td>0.3</td>
</tr>
<tr>
<td>Brisbane</td>
<td>3.1</td>
<td>3.3</td>
<td>3.6</td>
<td>0.8</td>
</tr>
<tr>
<td>Sydney</td>
<td>3.4</td>
<td>0.9</td>
<td>4.4</td>
<td>0.6</td>
</tr>
<tr>
<td>Melbourne</td>
<td>4.5</td>
<td>0.7</td>
<td>5.8</td>
<td>0.5</td>
</tr>
<tr>
<td>Kingaroy</td>
<td>2.8</td>
<td>1.2</td>
<td>3.7</td>
<td>0.8</td>
</tr>
<tr>
<td>Brigalow Research Station</td>
<td>3.4</td>
<td>1.0</td>
<td>4.4</td>
<td>0.9</td>
</tr>
<tr>
<td>Wagga Wagga</td>
<td>5.2</td>
<td>0.8</td>
<td>6.2</td>
<td>0.6</td>
</tr>
<tr>
<td>Bourke</td>
<td>2.8</td>
<td>3.9</td>
<td>3.9</td>
<td>1.1</td>
</tr>
<tr>
<td>Quilpie</td>
<td>3.5</td>
<td>1.1</td>
<td>4.6</td>
<td>0.7</td>
</tr>
<tr>
<td>Mount Isa</td>
<td>3.8</td>
<td>0.7</td>
<td>4.9</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Long-term droughts were most severe and prolonged in arid Quilpie (Table 2) and rare in temperate Melbourne. Likewise, severity and duration varied most at the two locations, together with arid Bourke. While severity and duration were moderately high in arid Mount Isa and temperate Brisbane, both parameters were low across the other selected temperate and tropical locations (Table 2).

No significant differences were detected ($p < 0.05$ at 95% confidence level) between RDI$_3$ and SPI$_3$, and SPEI$_{12}$ and SPI$_{12}$ (Fig. 5 and Appendix E). Correlation between RDI/SPEI and SPI was greatest for tropical Cairns and Weipa, and lowest for arid Bourke and Quilpie (outliers in Fig. 5). Interestingly, although Mount Isa was the most arid location ($R/PET = 0.13$, Table 1), the correlations between drought indices were relatively strong with values of 0.903 (Pearson’s $r$) and 0.759 (Kendall’s $\tau$) for long-term droughts.

For each location, the recurrence intervals of drought events exceeding any severity or duration of interest are depicted in Fig. 6 for short-term droughts (based on RDI$_3$) and Fig. 7 for long-term droughts (based on SPEI$_{12}$). Short-term droughts recurred most frequently in arid Mount Isa and were relatively rare in tropical Weipa and Cairns, and temperate Sydney. For example, in Mount Isa a drought with severity of 14 or duration of 17 months$^1$ recurred once in 50 years, whereas the same drought recurred only once in 100,000 years in Weipa, 300 years in Cairns, and 100 years in Sydney (Fig. 6). Long-term droughts recurred most frequently in arid Quilpie, where droughts with severity of 18 or duration of 10 months recurred once in 2 years. In Kingaroy and Sydney, the same drought recurred only once in 4 and 5 years, respectively (Fig. 7). Interestingly, although average long-term droughts were very severe and prolonged in Melbourne (Table 2), they only recurred once in 30 to 50 years. We found similar qualitative patterns in all locations for recurrence intervals of droughts exceeding any severity and duration of interest (Appendix D).

4 Discussion

In this study we estimated the recurrence intervals of short- and long-term droughts based on meteorological drought indices and copulas (i.e. bivariate probability distributions). For both timescales, the correlation between the simple SPI (rainfall) and the more complex SPEI or RDI (rainfall and evaporation) was much stronger for the tropical and temperate locations (e.g. Cairns, Weipa, Brigalow) than for the arid locations in severity was detected in arid Bourke and temperate Brisbane (Table 1).

Long-term droughts were most severe and prolonged in arid Quilpie (Table 2) and rare in temperate Melbourne. Likewise, severity and duration varied most at the two locations, together with arid Bourke. While severity and duration were moderately high in arid Mount Isa and temperate Brisbane, both parameters were low across the other selected temperate and tropical locations (Table 2).

No significant differences were detected ($p < 0.05$ at 95% confidence level) between RDI$_3$ and SPI$_3$, and SPEI$_{12}$ and SPI$_{12}$ (Fig. 5 and Appendix E). Correlation between RDI/SPEI and SPI was greatest for tropical Cairns and Weipa, and lowest for arid Bourke and Quilpie (outliers in Fig. 5). Interestingly, although Mount Isa was the most arid location ($R/PET = 0.13$, Table 1), the correlations between drought indices were relatively strong with values of 0.903 (Pearson’s $r$) and 0.759 (Kendall’s $\tau$) for long-term droughts.

For each location, the recurrence intervals of drought events exceeding any severity or duration of interest are depicted in Fig. 6 for short-term droughts (based on RDI$_3$) and Fig. 7 for long-term droughts (based on SPEI$_{12}$). Short-term droughts recurred most frequently in arid Mount Isa and were relatively rare in tropical Weipa and Cairns, and temperate Sydney. For example, in Mount Isa a drought with severity of 14 or duration of 17 months$^1$ recurred once in 50 years, whereas the same drought recurred only once in 100,000 years in Weipa, 300 years in Cairns, and 100 years in Sydney (Fig. 6). Long-term droughts recurred most frequently in arid Quilpie, where droughts with severity of 18 or duration of 10 months recurred once in 2 years. In Kingaroy and Sydney, the same drought recurred only once in 4 and 5 years, respectively (Fig. 7). Interestingly, although average long-term droughts were very severe and prolonged in Mel-

---

$^1$Drought events are calculated by 3-month (short-term) and 12-month (long-term) running precipitation totals (Guttman, 1999).
locations (e.g. Quilpie, Bourke, Wagga Wagga). Extending a former study on abiotic boundaries affecting ecological development of post-mining landscapes (Audet et al., 2013), our findings have critical implications for assessments of rehabilitation success.

### 4.1 Implications for ecosystem rehabilitation planning

Across eastern Australia, current post-mining land rehabilitation strategies often do not incorporate site-specific rainfall and drought metrics other than the average annual rainfall depth (Audet et al., 2013). However, regionally extreme rainfall patterns, including both intense rainfall events such as storms or cyclones and prolonged periods of water deficit (droughts), play a critical role in identifying windows of opportunity and/or challenge to the rehabilitation of early-establishment ecosystems (Hinz et al., 2006; Hodgkinson et al., 2010). Furthermore, Audet et al. (2013) suggested that short and long-term ecosystem rehabilitation sensitivity to climate can be effectively determined by the seasonality, regularity, and intensity of weather, combined with both median and standard deviation of periods. In particular, prolonged seasonal drought with high variation and frequently occurring intense rainfall can be used as primary characteristics.
for determining site sensitivity, while regular rainfall and relatively short periods of water deficit are common characteristics of favourable climate conditions. Based on their findings, Audet et al. (2013) revealed how broad scale rainfall patterns outline climate boundaries that drive rehabilitation sensitivity in arid to temperate locations across eastern Australia. For example, ecosystem rehabilitation in arid regions (Mount Isa, Quilpie, and Bourke) is sensitive to climate as they have highly variable climates (long spell of droughts and high intensity rainfall), which affect the success of rehabilitation.

Commonly, the characterisation of climatic conditions is based on long-term rainfall and does not consider short and long-term drought conditions. Identifying drought and its variables are critical factors in ecosystem rehabilitation because the distribution and health of plant species are vulnerable to droughts and plant available water (Engelbrecht et al., 2007). In our study we presented two hydrological parameters describing the average recurrence intervals of short-term and long-term droughts (Figs. 6 and 7 and Appendix D), which can be used instead of the oversimplified parameters of the median period without rain and standard deviation normally used (Audet et al., 2013).

The design drought tool proposed in this paper is an adaptation of the intensity–duration–frequency (IDF) analysis of rainfall events, a standard tool used by engineers (Haile-
Table 3. Management actions for addressing specific kinds of drought characteristics identified with SDF curves for the southern hemisphere.

<table>
<thead>
<tr>
<th>Management domain</th>
<th>Management actions</th>
<th>Type of drought</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plant species selection</td>
<td>Drought tolerant species</td>
<td>LS, LP, SP, SS</td>
</tr>
<tr>
<td></td>
<td>Quickly germinating species</td>
<td>SS</td>
</tr>
<tr>
<td></td>
<td>Species with physical/chemical dormancy</td>
<td>LS, LP</td>
</tr>
<tr>
<td></td>
<td>Shade tolerant species on southern aspects</td>
<td>LS, LP</td>
</tr>
<tr>
<td></td>
<td>Light tolerant species on northern aspects</td>
<td>LS, LP, SP, SS</td>
</tr>
<tr>
<td></td>
<td>Annual grasses</td>
<td>SS, SP</td>
</tr>
<tr>
<td></td>
<td>Perennial grasses</td>
<td>LS, LP, SP, SS</td>
</tr>
<tr>
<td></td>
<td>Trees</td>
<td>LS, LP</td>
</tr>
<tr>
<td>Planting/seeding regime</td>
<td>Trees require repeated establishment</td>
<td>LS, LP</td>
</tr>
<tr>
<td></td>
<td>Annual/perennial grasses are successful after rain events</td>
<td>SS, SP</td>
</tr>
<tr>
<td>Soil characteristics</td>
<td>Deep topsoil</td>
<td>LS, LP, SP</td>
</tr>
<tr>
<td></td>
<td>Amendments of silt/clay</td>
<td>LS, LP</td>
</tr>
<tr>
<td></td>
<td>Gentle slopes</td>
<td>LS, LP</td>
</tr>
<tr>
<td></td>
<td>Mulching</td>
<td>SS</td>
</tr>
<tr>
<td>Irrigation method</td>
<td>Regular irrigation</td>
<td>LS, LP</td>
</tr>
<tr>
<td></td>
<td>Seasonal irrigation</td>
<td>SS, SP</td>
</tr>
<tr>
<td></td>
<td>Critical stage irrigation</td>
<td>LS, LP, SP, SS</td>
</tr>
<tr>
<td></td>
<td>Drainage system</td>
<td>LS, LP</td>
</tr>
</tbody>
</table>

SS – high recurrence of short term (3 months) severe droughts; SP – high recurrence of short term (3 months) prolonged droughts; LS – high recurrence of long term (12 months) severe droughts; LP – high recurrence of long term (12 months) prolonged droughts.

Our new term “design droughts”, characterised by drought severity–duration–frequency (SDF), is based on the severity of droughts (cumulative negative values of a particular drought; see Fig. 3) as opposed to IDF, which is based on the intensity of the rainfall. Design droughts allow for drought severity, duration and frequency to be considered in order to determine the risk of failure of current mining operations (Mason et al., 2013; Burton et al., 2012), and to design robust ecosystem components in the face of the local climate variability (Audet et al., 2013). Unlike degraded land (in the sense of gradual loss of ecosystem productivity) in post-mining landscapes, most ecosystem components are impacted by mining activities; particularly landform, hydrology, and ecosystem structure (Arnold et al., 2014b). Therefore, successful rehabilitation of post-mining land requires the sensible selection of plant species, as well as planting/seeding regime, soil characteristics, irrigation method, and landform characteristics (Table 3). For example, same vegetation types cannot establish if a drought event exceeds values of specific duration or severity (Arnold et al., 2014a). The recurrence intervals can provide the probability of a drought occurring at this duration or severity, and thus the risk of establishment failure can be assessed. This is important for rehabilitation managers who can conduct a cost–benefit analysis to decide whether the costs of constructing mitigation methods (such as irrigation) are comparable with the costs of potential failure of multiple revegetation attempts.

Together, design rainfalls (IDF) and droughts (SDF) should be the primary determinants of rehabilitation strategies and eventually help guide rehabilitation planning, where environmental conditions have an impact on current mining operations. In accordance with IDF parameters of similar locations across eastern Australia (Audet et al., 2013), temperate and tropical environmental conditions (Table 1) are favourable for rehabilitation, i.e. recurrence intervals of droughts are large (Figs. 6 and 7 and Appendix D). By contrast, re-establishment of ecosystems are prone to failure in arid conditions, where droughts recur more frequently (i.e. low recurrence intervals).

At locations with distinct patterns of winter and summer rainfall, such as Weipa, Cairns, Mount Isa, or the Brigalow Belt, seasonality is the primary determinant of drought occurrence (Table 1). The short-term drought index (RDI) detects most severe and prolonged droughts in tropical Weipa and Cairns (Table 2), where rainfall is low in winter and high in summer. Annual recurring seasonal patterns also explain the low variability of short-term drought severity and duration. In contrast the long-term drought index (SPEI) detects most severe and prolonged droughts in arid Quilpie and Mount Isa, as well as temperate Melbourne (Table 2). Major weather events such as El Niño and La Niña from recent decades coincided with low and high drought indices, respectively (Fig. 4 and Appendix C).

We compared SPI with SPEI or RDI to determine the potential of using SPI (only based on rainfall data) over SPEI.
or RDI (both based on rainfall and evaporation data). This might be of interest for many parts of the world, where evaporation data are unavailable or incomplete and therefore simple rainfall indices are most commonly used. Our analysis revealed that Pearson’s $r$ and Kendall’s $\tau$ correlations were strong across selected locations (Fig. 5 and Appendix E), indicating the potential of the simple SPI to serve as a surrogate for the more complex RDI and SPEI. For temperate and tropical environments, such as Cairns, Weipa, or Brisbane, the more complex RDI and SPEI can be replaced by the simple SPI if evaporation data is not available (Fig. 5 and Appendix E). By contrast, in arid Bourke, Quilpie, or Mount Isa, correlations between SPI and the more complex indices were weaker, because evaporation plays a critical role in arid climates rather than in tropics and temperate regions. In these arid and water-limited locations (Table 1) we recommend using SPEI and RDI2 and also to conduct intensive monitoring of ecosystem development in relation to empirical weather data to measure evaporation directly, e.g. pan evaporation (Lugato et al., 2013; Clark, 2013), or indirectly, e.g. based on radiative and aerodynamic variables (Allen et al., 1998).

4.2 SDF curves as an early risk assessment tool

Risk assessment based on the design rainfall concept is commonly used as a standard tool by engineers to design infrastructure such as storm water drains, flood mitigation levees, or retarding dams (Chebbi et al., 2013; Hailegeorgis et al., 2013). This research paper aims to demonstrate how these concepts can be used for ecosystem rehabilitation, providing a quantitative estimate of ecosystem rehabilitation failure due to water deficit. Traditionally, ecologist and land managers often use the mean annual rainfall as a co-classifier of biogeographic regionalisation. However, annual rainfall alone cannot account for the vulnerability of a site to non-disruptive water supply, the frequency of water limitations, and seasonality (Audet et al., 2013). For example, although mean annual rainfall is lowest in Bourke, the SDF analysis reveals that severe and prolonged droughts occur most frequently in Mount Isa. This is because in Mount Isa on average 23 out of 100 days are with no rainfall, as most of the rainfall occurs in summer as storm events greater than 100 mm (Table 1) (Bureau of Meteorology, 2013). Ecosystem rehabilitation may fail if management actions are based only on the annual rainfall without considering the nature of drought events (i.e. the rate of recurrence of prolonged and severe droughts) (Table 3).

Quantitatively, risk is the product of the probability of an event occurring and the consequences of an event on assets (Athearn, 1971). In the context of post-mining land rehabilitation, the recurrence intervals quantify the probability of occurrence of drought events. If the consequences of drought events for ecosystems are known (Wilhite et al., 2007; Williamson et al., 2000) the risk of ecosystem rehabilitation failure can be quantified. Consequences will typically have to be determined in relation to site specific attributes such as plant species, soil, irrigation, etc. (Table 3). Likewise, the consequences can also be related to the costs of rehabilitation. For example, for frequently recurring droughts of high severity and duration, irrigation may be a cost-efficient alternative to repeatedly replanting at a rehabilitation site due to establishment failure. These consequences in relation to severity and duration may be identified from the literature, field trials or be derived from expert opinion. A key aspect of our study is that SDF curves provide the probability of occurrence of drought events with a specific duration and severity.

4.3 Application of design droughts to rehabilitation planning

One of the major outcomes of this study is to support land managers and/or rehabilitation practitioners to make fundamental decisions on appropriate management actions in the context of drought frequency. For rehabilitation to be successful in the face of severe and prolonged droughts, there are a range of management domains and management actions that need to be considered in response to recurrence intervals, drought severity, and drought duration (Table 3). These management actions can be categorised into four domains: plant species selection; planting/seeding regime; soil characteristics; and irrigation method.

Meteorological droughts indicate deviations of rainfall and/or evaporation relative to the long-term average. Native climax vegetation, which is well adapted to the local climate, is hardly sensitive to these anomalies. However, within the process of post-mining land rehabilitation, establishment of well-adapted climax vegetation is impossible. In fact, post-mining ecosystem rehabilitation is very sensitive to decisions made on the re-established topography and soil characteristics, as well as planting/seeding regimes and irrigation methods (Table 3). In this regard, the frequency of meteorological droughts relative to long-term conditions is the critical driver of these management decisions. For example, seedling establishment might fail under conditions of frequently occurring short-term droughts, even if the absolute rainfall in between droughts is high. Under these conditions, landform and soil need to be restored so that the periods of water limitation can be minimised.

Selection of suitable plant species based on drought type is one of the key management actions for successful rehabilitation. Some management actions can be applied to all drought types (LS, LP, SS, SP in Table 3). These include (i) planting of drought tolerant species (e.g. Acacia spp., Banksia spp., Casuarina spp.) at (ii) northern aspects to address drier conditions that result from higher solar radiation causing increased evaporation (Sternberg and Shoshany, 2001), and...
(iii) planting of perennial grasses (Eragrostis spp., Themeda spp.; Bolger et al., 2005), which may not be affected by long-term water deficits. At locations with frequently recurring long-term (12-monthly timescale) droughts of high severity and durations (LS, LS in Table 3), e.g. in Mount Isa and Quilpie, seeding of species with physical/chemical dormancy may increase the probability of germination during favourable periods (Hilhorst, 1995; Arnold et al., 2014b). Additionally, a southern aspect may require drought tolerant species to increase survival of plant communities (Sternberg and Shoshany, 2001). However, these species need to be shade tolerant as southern aspects get less solar radiation in winter. At locations with frequently recurring short-term (3-monthly timescale) droughts of high severity but short duration, with rainfall throughout the year (SS in Table 3), e.g. in Wagga Wagga, annual grasses and seeds with short germination periods may be suitable.

Soil characteristics play a critical role for plant available water and a number of strategies may need to be employed to make soil more favourable to plant establishment. Except for mulching, all soil management actions can be applied to locations with high recurrence of long-term, severe, and prolonged droughts (LS, LS in Table 3), e.g. in Quilpie and Mount Isa. For locations with high recurrence of short-term, and prolonged droughts (SP in Table 3), such as Melbourne, increasing depth of topsoil can increase water holding capacity (Audet et al., 2013; Bot and Benites, 2005). Similarly, by mixing silt and clay soil in the topsoil and reducing slope gradients may facilitate infiltration and increase soil water retention capacity (Audet et al., 2013). For tropical locations with high recurrence of short-term (3-monthly timescale), severe, and prolonged droughts (SS, SP in Table 3), e.g. in Cairns and Weipa, ground cover such as mulch and fast growing vegetation cover (e.g. Buffel grass) may reduce evaporation and maintain soil moisture to facilitate the establishment of drought sensitive and slow growing species (Blum, 1996).

Utilising irrigation methods for specific site characteristics is a cost-effective strategy for any rehabilitation plan. Regular irrigation with proper drainage systems that distributes water is an effective strategy in locations with high recurrence of long-term, severe, and prolonged droughts (LP, LS in Table 3). For locations with high recurrence of short-term, severe, and prolonged droughts (SS, SP in Table 3), with seasonal rainfall (e.g. Brisbane, Sydney, Kingaroy, Brigalow), seasonal irrigation and irrigation at critical stages of plant growth (Blum, 1996), such as during periods of germination, and root or pod development periods are efficient actions to ensure plant survival throughout drought spells.

4.4 Future research

The method outlined in this study provides a useful tool for land managers to address site-based climatic conditions. Future research needs to build on this tool, as well as address the limitations of our method based on meteorological drought indices inferred from point observations. This research may assess: (i) the relationship between meteorological and agricultural drought indices; (ii) regional scale mapping of drought indices; and (iii) the predictive power of design droughts.

While the applied drought indices are robust indicators of meteorological droughts (Mishra and Singh, 2010; Quiring, 2009), they are limited to detecting anomalies from historic rainfall patterns. Soil plays a critical role for any ecosystem development, particularly with regard to ecosystem rehabilitation in post-mining land (Arnold et al., 2013), as soil properties translate rainfall into plant available water (Zhang et al., 2001; Huang et al., 2013). Future drought analysis would benefit from integrating soil properties such as depth, texture, salinity, or organic matter content into drought indices to describe agricultural droughts (Khare et al., 2013; Baldocchi et al., 2004; Woli et al., 2012). Soil texture and depth are critical factors in highly seasonal climates, where soil water storage overcomes periods of water deficit (Prentice et al., 1992; Bot and Benites, 2005). However, using simple and easily accessible meteorological data is a critical step forward to making it easier for mine rehabilitation managers to adopt the concept of using SDF curves as early risk assessment tools.

Although the selected locations can be considered representative of the agro-climatic environments across eastern Australia (Fig. 1), our analysis is strictly valid for the selected point data and therefore site-specific. Future work should not only integrate the above-mentioned soil component but also extend drought analyses across Australia using gridded weather data from the Bureau of Meteorology (2014). Future investigations could assess possible trends in temporal changes of recurrence intervals by dividing historic time series of rainfall and evaporation into subsets and replicate the analysis for each subset (Li et al., 2014; Darshana et al., 2013; Jacobs et al., 2013; Halwatura et al., 2015).

5 Conclusions

The study revealed site-specific patterns of recurrence intervals of short-term and long-term droughts across eastern Australia. Severe and prolonged short-term droughts recur most often in tropical climates and temperate Wagga Wagga, while severe and prolonged short-term droughts recur most often in arid conditions and temperate Melbourne. Design droughts can be applied to quantify the frequency of drought events – characterised by severity and duration – at different timescales. This is a critical step forward to consider drought in risk assessments for rehabilitation of post-mining ecosystems. Together with design rainfalls, design droughts should be used to assess rehabilitation strategies and ecological management based on drought recurrence intervals, thereby minimising the risk of failure of initial ecosystem establishment due to ignorance of fundamental abiotic and site-specific environmental barriers.
Appendix A: RDI and SPEI

A1 RDI

The standardised RDI is given as

\[ RDI_{st}(k) = \frac{y_k - \bar{y}_k}{\hat{\sigma}_k}, \]  

(A1)

with

\[ y_k = \ln \left( \sum_{j=1}^{j=k} P_j \right) \]  

(A2)

where \( \hat{\sigma} \) is the standard deviation, \( y_k \) is month \( k \) of year \( y \), \( \bar{y}_k \) is the arithmetic mean of \( y_k \), \( \hat{\sigma}_k \) is the standard deviation of \( y_k \), and \( P_j \) and \( PET_j \) are precipitation and potential evapotranspiration for the \( j \)th month of the hydrological year, respectively (Tsakiris and Vangelis, 2005).

A2 SPEI

The SPEI is calculated as

\[ SPEI = W - \frac{C_0 + C_1 W + C_2 W^2}{1 + d_1 W + d_2 W^2 + d_3 W^3}, \]  

(A3)

with

\[ W = \sqrt{-2 \ln(P)} \]  

for \( P \leq 0.5 \),

(A4)

where \( P \) is the probability of exceeding a determined value of the difference between the precipitation and potential evapotranspiration \( (P = 1 - F(x)) \). If \( P > 0.5 \), then \( P \) is replaced by \( 1 - P \) and the sign of the resultant SPEI is reversed. The constants are \( C_0 = 2.515517, \) \( C_1 = 0.802853, \) \( C_2 = 0.010328, \) \( d_1 = 1.432788, \) \( d_2 = 0.189269, \) and \( d_3 = 0.001308 \) (Vicente-Serrano et al., 2010).

Appendix B: Mathematical description of Gumbel and Frank copula (Shiau, 2006)

B1 Gumbel copula

\[ C(u, v) = \exp \left\{ \frac{-1}{\theta} \left( \left( -\ln u \right)^\theta + \left( -\ln v \right)^\theta \right)^{\frac{1}{\theta}} \right\}, \]  

\( \theta \geq 1 \) (B1)

\[ c(u, v) = C(u, v) \left( \frac{1}{uv} \right)^{\frac{1}{\theta}} \left( \left( -\ln u \right)^\theta + \left( -\ln v \right)^\theta \right)^{\frac{2}{\theta} - 2} \cdot \left( \theta - 1 \right) \]  

(B2)

B2 Frank copula

\[ C(u, v) = -\frac{1}{\theta} \ln \left[ 1 + \left( \frac{e^{-\theta u} - 1}{e^{\theta - 1}} \right) \left( \frac{e^{-\theta v} - 1}{e^{\theta - 1}} \right) \right], \]  

\( \theta \neq 0 \) (B3)

\[ c(u, v) = -\frac{\theta e^{-\theta (u+v)} \left( e^{-\theta} - 1 \right)}{\left( e^{-\theta (u+v)} - e^{-\theta u} - e^{-\theta v} + e^{-\theta} \right)^2} \]  

(B4)
Appendix C: Time series of drought indices and major weather event

Figure C1. Calculated SPEI$_{12}$ for selected locations across eastern Australia.

Figure C2. Calculated RDI$_3$ for selected locations across eastern Australia.
Appendix D: Recurrence intervals of drought events with any severity and duration of interest

Figure D1. Recurrence intervals $T^\wedge$ (years) of drought events with any severity and duration of interest based on RDI$_3$ (short-term) of historical rainfall.
Figure D2. Recurrence intervals $T^\wedge$ (years) of drought events with any severity and duration of interest based on SPEI$_{12}$ (long-term) of historical rainfall.
### Table E1. Coefficient values of Pearson’s $r$ and Kendall’s $\tau$ for SPI$_3$ vs. RDI$_3$, and SPI$_{12}$ vs. SPEI$_{12}$. Correlations were lowest for arid Bourke and Quilpie (bold values).

<table>
<thead>
<tr>
<th>Location</th>
<th>SPI$_3$ vs. RDI$_3$</th>
<th>SPI$<em>{12}$ vs. SPEI$</em>{12}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Pearson’s $r$</td>
<td>Kendall’s $\tau$</td>
</tr>
<tr>
<td>Weipa</td>
<td>0.98</td>
<td>0.92</td>
</tr>
<tr>
<td>Cairns</td>
<td>0.98</td>
<td>0.90</td>
</tr>
<tr>
<td>Brisbane</td>
<td>0.81</td>
<td>0.62</td>
</tr>
<tr>
<td>Sydney</td>
<td>0.82</td>
<td>0.61</td>
</tr>
<tr>
<td>Melbourne</td>
<td>0.98</td>
<td>0.90</td>
</tr>
<tr>
<td>Kingaroy</td>
<td>0.77</td>
<td>0.54</td>
</tr>
<tr>
<td>Bragalo</td>
<td>0.90</td>
<td>0.71</td>
</tr>
<tr>
<td>Wagga Wagga</td>
<td>0.69</td>
<td>0.68</td>
</tr>
<tr>
<td>Bourke</td>
<td><strong>0.43</strong></td>
<td><strong>0.54</strong></td>
</tr>
<tr>
<td>Quilpie</td>
<td><strong>0.57</strong></td>
<td><strong>0.40</strong></td>
</tr>
<tr>
<td>Mount Isa</td>
<td>0.78</td>
<td>0.60</td>
</tr>
</tbody>
</table>
Appendix F: $R^2$ and $p$ values for fitted cumulative distribution functions and Copula parameters

Table F1. $R^2$ and $p$ values for fitted cumulative distribution functions and Copula parameters for the studied sites.

<table>
<thead>
<tr>
<th>Station</th>
<th>Cumulative distribution functions</th>
<th>Copula</th>
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<tbody>
<tr>
<td></td>
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<td>Logistic</td>
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<tr>
<td></td>
<td>$R^2$</td>
<td>$p$</td>
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<tr>
<td>Brisbane</td>
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<td>0.30</td>
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<tr>
<td>Sydney</td>
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<td>0.00</td>
</tr>
<tr>
<td>Melbourne</td>
<td>0.25</td>
<td>0.00</td>
</tr>
<tr>
<td>Kingaroy</td>
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<td>Brigalow</td>
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<td>Wagga Wagga</td>
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<tr>
<td>Quilpie</td>
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<td>0.00</td>
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<tr>
<td>Mount Isa</td>
<td>0.20</td>
<td>0.00</td>
</tr>
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</table>
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